NS 102 Lecture 13 May 12, 2005

The Shroud of Vegas

Open: *Staring at the Sun*
TV on the Radio
Close: *Burning Love*
Elvis

GnatSigh News

(all the news that fits)

- **Website**

  http://home.fnal.gov/~rocky/NS102/

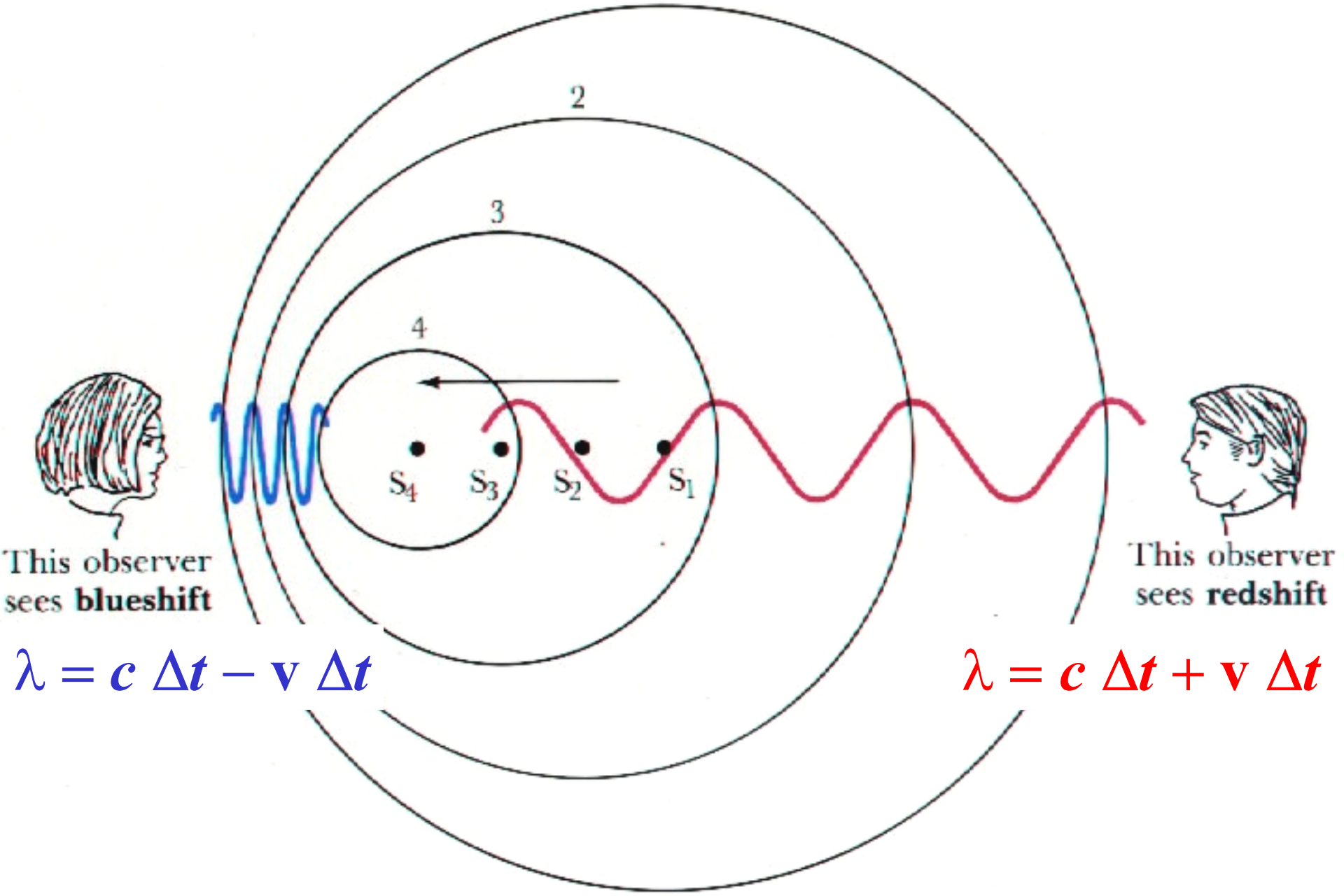
- **Today: The death of Elvis**

  http://girlsguidetoelvis.com/deathofelvis.html

- **Carbon-14 dating:**

  http://science.howstuffworks.com/carbon-14.htm

Lab this week: Geometry of the Universe


2
3
4
S_4
S_3
S_2
S_1
This observer sees **blueshift**
This observer sees **redshift**
$\lambda = c\,\Delta t - v\,\Delta t$
$\lambda = c\,\Delta t + v\,\Delta t$

Doppler Shift

$\lambda_0 =$ rest wavelength

$\lambda =$ detected wavelength

$$\lambda = \lambda_0 \left(1 \pm \frac{v}{c} \right)$$

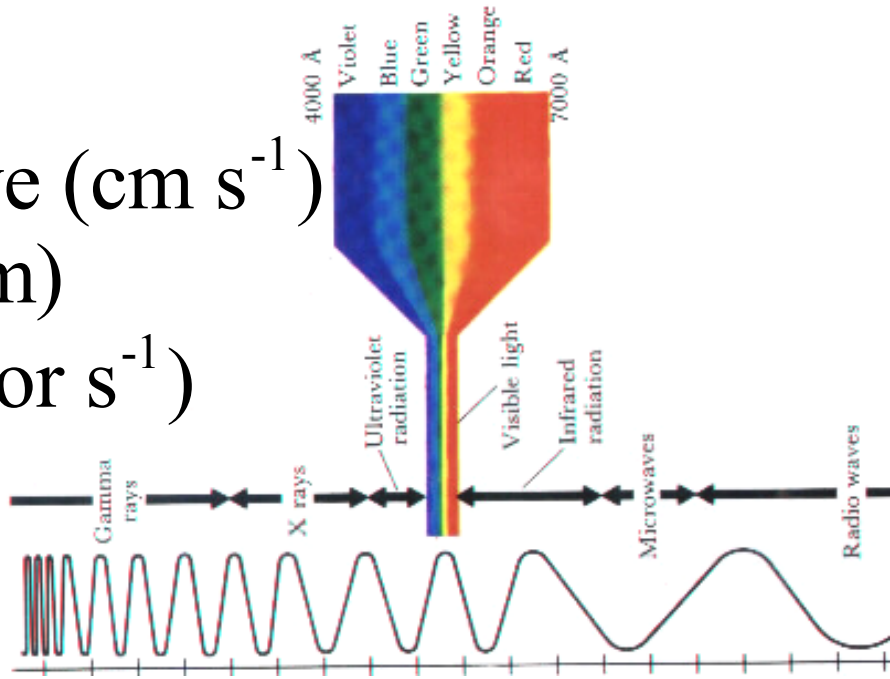
$+ \rightarrow$ receding (longer λ)

$- \rightarrow$ approaching (shorter λ)

Facts about light

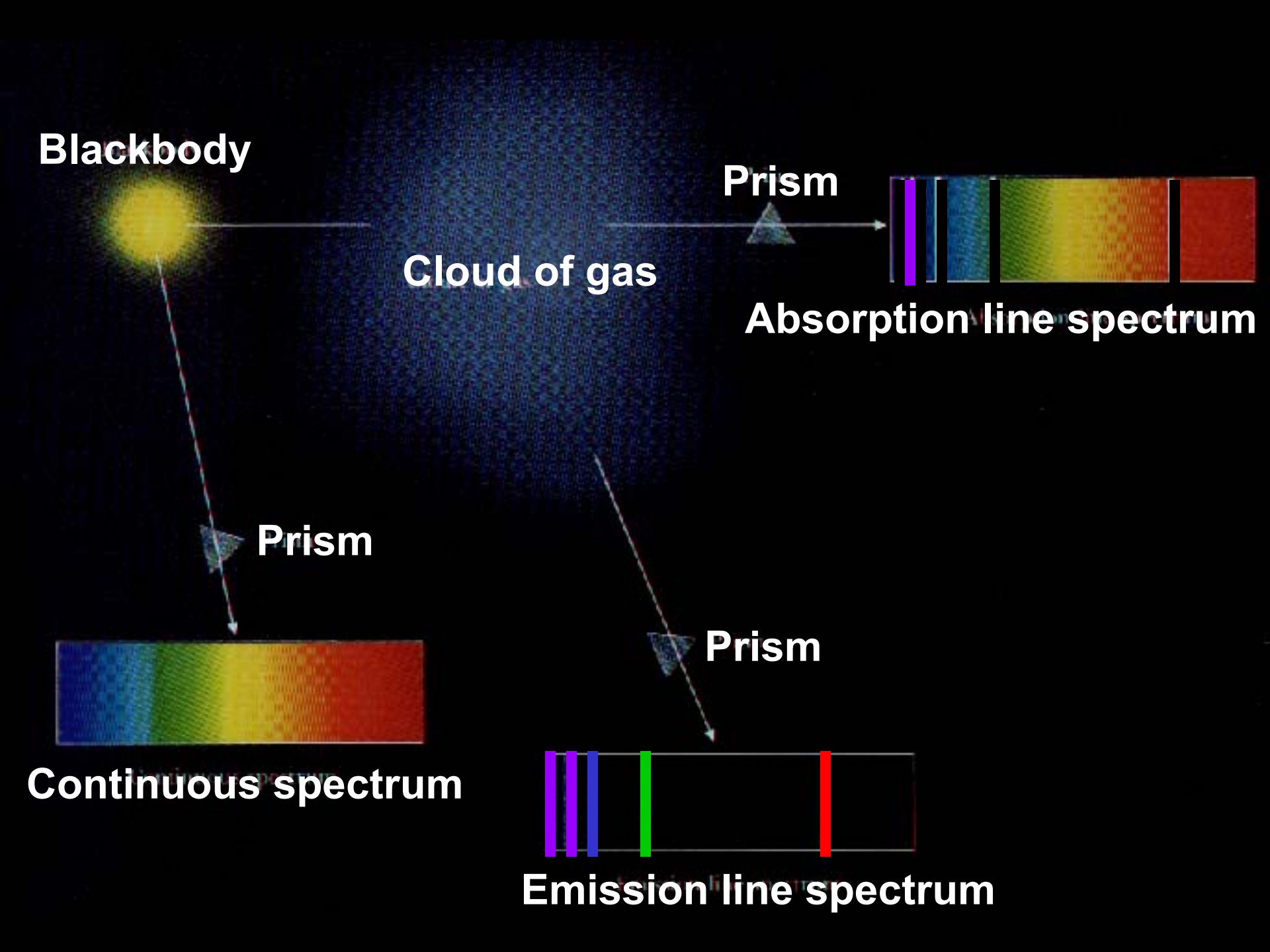
1. Light is a wave

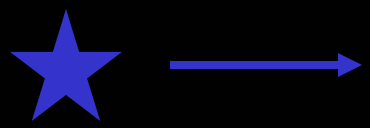
$$c = \lambda \nu \quad \begin{cases} c = \text{ velocity of wave (cm s}^{-1}) \\ \lambda = \text{ wavelength (cm)} \\ \nu = \text{ frequency (Hz or s}^{-1}) \end{cases}$$



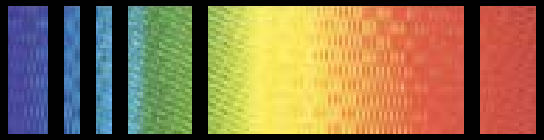
2. The wavelength is quantized

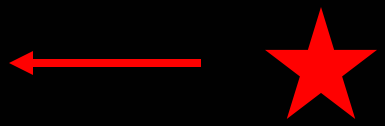
Visible Emission Spectrum

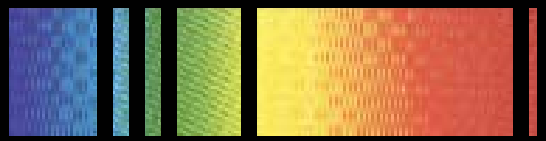

Blackbody
Prism
Cloud of gas
Absorption line spectrum
Prism
Prism
Continuous spectrum
Emission line spectrum



blue shift

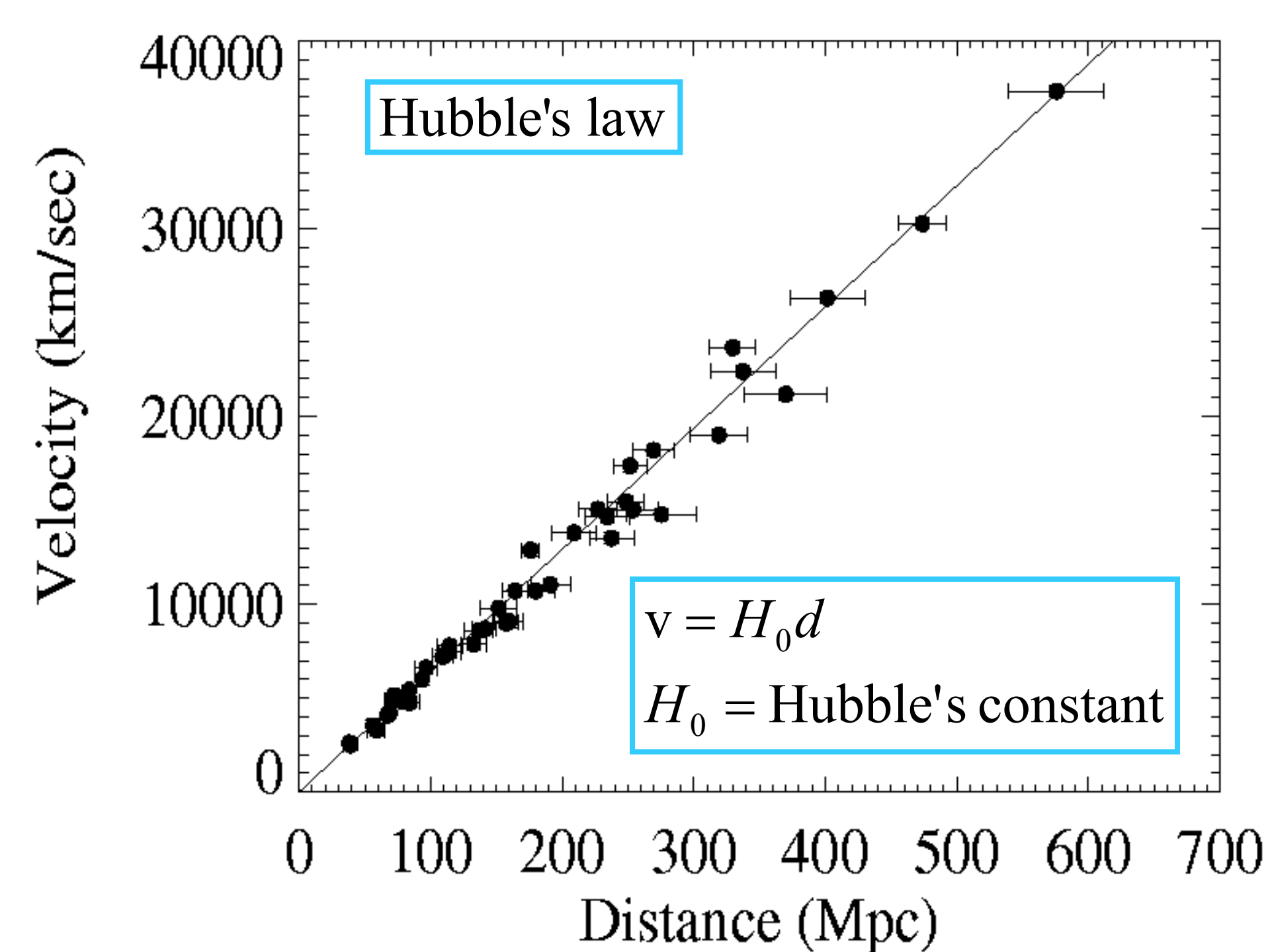






red shift

Edwin Hubble
1884 - 1953


Hubble's law
$v = H_0 d$
H_0 = Hubble's constant
Velocity (km/sec)
40000
30000
20000
10000
0
0
100
200
300
400
500
600
700
Distance (Mpc)

$$v = H_0 d$$

H_0 = Hubble's constant

Let's assume $H_0 = 100\ \text{km s}^{-1}\ \text{Mpc}^{-1}$

$$v = 100 \frac{\text{km}}{\text{s}} \frac{d}{\text{Mpc}}$$

v	d
$100\ \text{km s}^{-1}$	1 Mpc
$1{,}000\ \text{km s}^{-1}$	10 Mpc
$10{,}000\ \text{km s}^{-1}$	100 Mpc
$100{,}000\ \text{km s}^{-1}$	1,000 Mpc

$$\lambda = 6{,}000 \ \text{Angstroms}$$

$$\lambda_0 = 5{,}000 \ \text{Angstroms}$$

$$\frac{\mathrm{v}}{c} = \frac{\lambda - \lambda_0}{\lambda_0} = \frac{1000}{5000} = 0.2$$

$$\mathrm{v} = 0.2c \ \Rightarrow \ \mathrm{v} = 60{,}000 \ \mathrm{km\ s^{-1}}$$

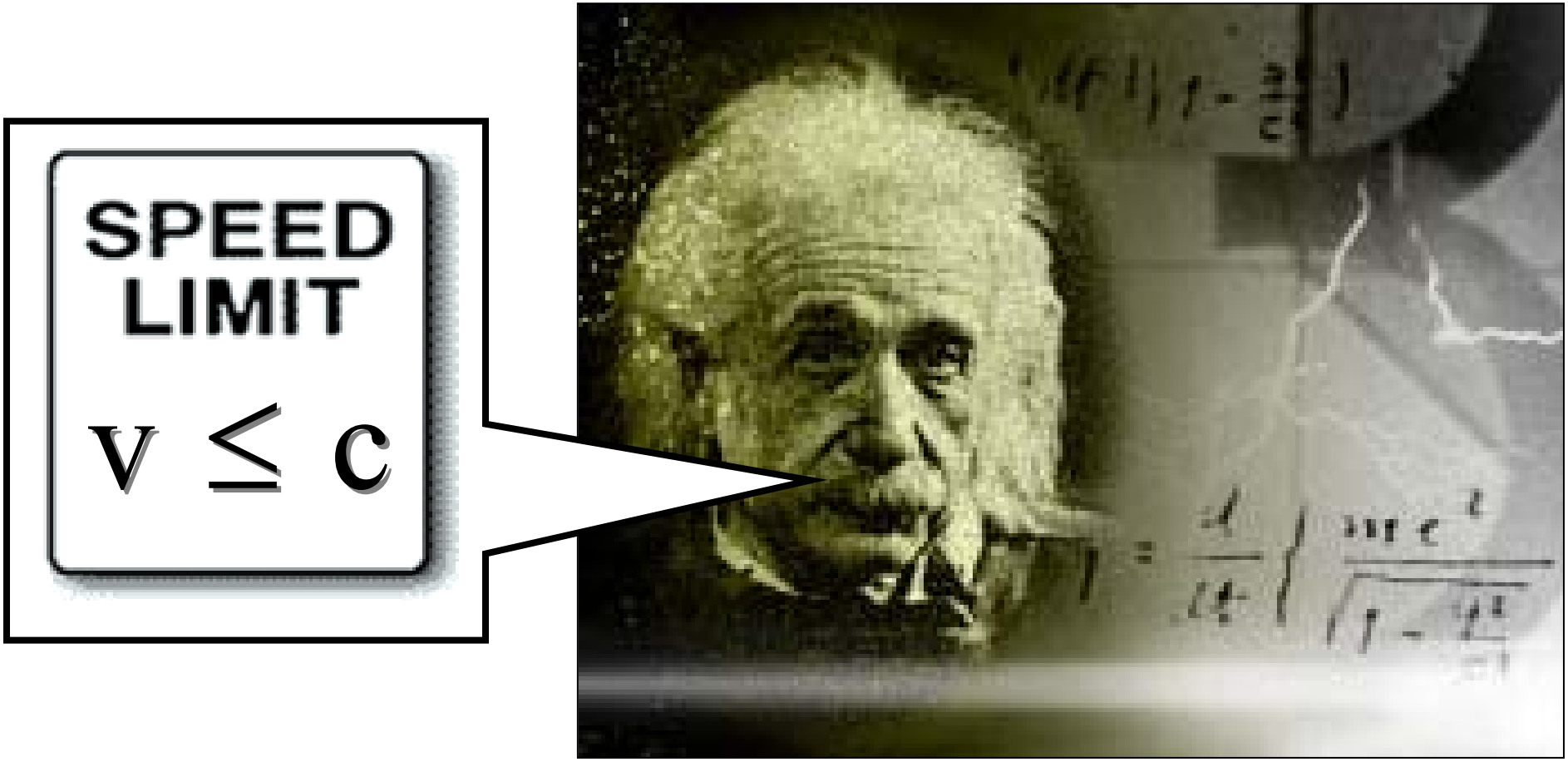
$$\lambda = 15,000 \text{ Angstroms}$$

$$\lambda_0 = 5,000 \text{ Angstroms}$$

$$\frac{\mathrm{v}}{c} = \frac{\lambda - \lambda_0}{\lambda_0} = \frac{10,000}{5,000} = 2$$

$$\mathrm{v} = 2c \quad \Rightarrow \quad \mathrm{v} = 600,000 \text{ km s}^{-1}$$

$$c = 300,000 \text{ km s}^{-1}$$



Relativistic redshift equation

$$z = \frac{\lambda - \lambda_0}{\lambda_0}$$

$$\frac{v}{c} = \frac{(z+1)^2 - 1}{(z+1)^2 + 1} = \frac{z^2 + 2z}{z^2 + 2z + 2}$$

$$\approx \frac{2z}{2} = z = \frac{\lambda - \lambda_0}{\lambda_0} \qquad (z << 1)$$

$$\approx \frac{z^2}{z^2} = 1 \qquad (z >> 1)$$

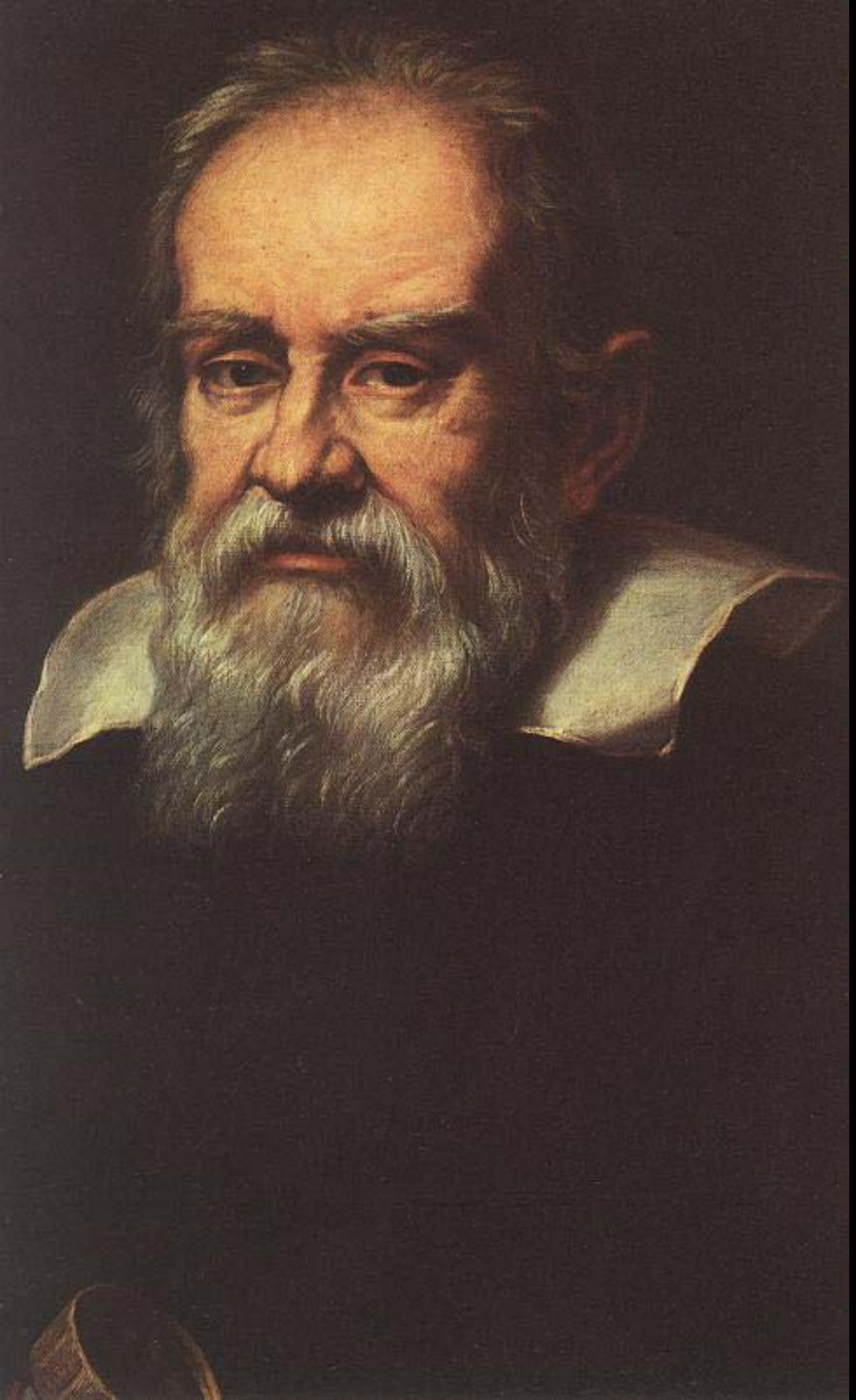
We are not the center of the expansion of the universe

Every galaxy sees the expansion

Cosmological Principle

The universe is the same everywhere

- no special point in the universe (no center)
- no special set of points (no edge)



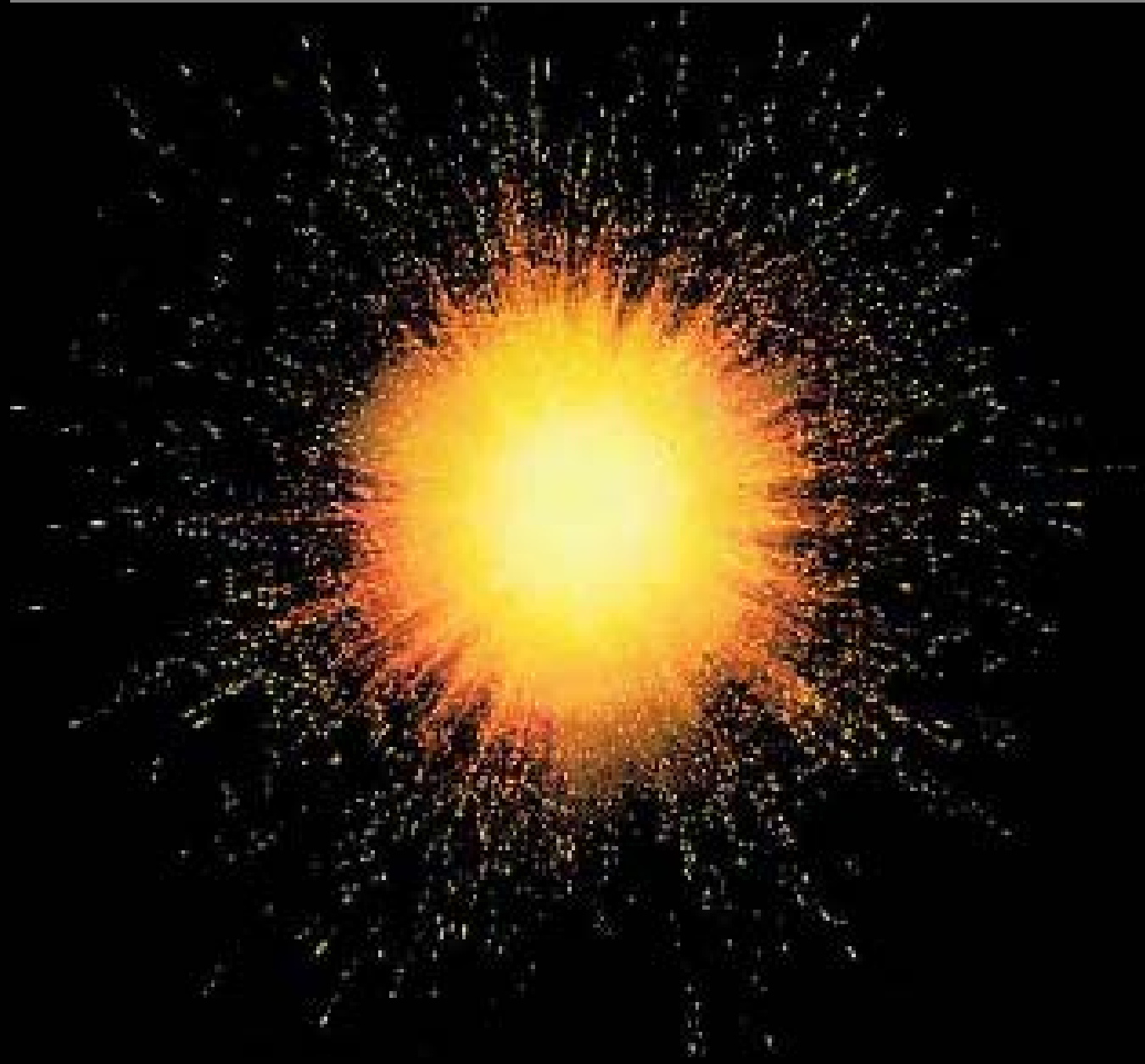
Galileo on the center of the universe, from *Dialog Concerning the Two Chief World Systems*

SALVIATI: ***Ancorché molto ragionevolmente io potessi mettervi in controversia…*** I might very reasonably dispute whether there is in nature such a center, seeing that neither you nor anyone else has so far proved whether the universe is finite and has a shape, or whether it is infinite and unbounded. …But I shall concede to you for the time being that the universe is finite, spherical, and has a center.

In the field of modern cosmology, the first principle is called the “Cosmological Principle. It states that the universe has no center, that it has the same properties throughout. Every place in the universe has, in this sense, equal rights. How can the human race, which has evolved in a universe of such fundamental equality, fail to strive for a society without violence and terror? How can we fail to build a world in which the rights of every human from birth are respected?

Fang Li Zhi
Acceptance speech
for the
Robert F. Kennedy
Memorial Human
Rights Award

This is not the big bang!

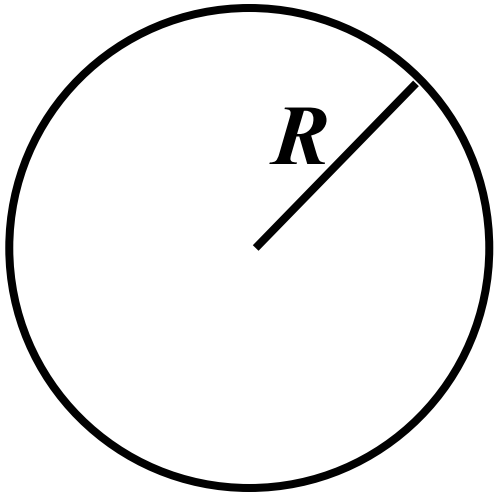


Spaces that obey the cosmological principle:

1-dimension:

^1R  x

$$V = \int_{-\infty}^{\infty} dx = \infty$$

^1S 

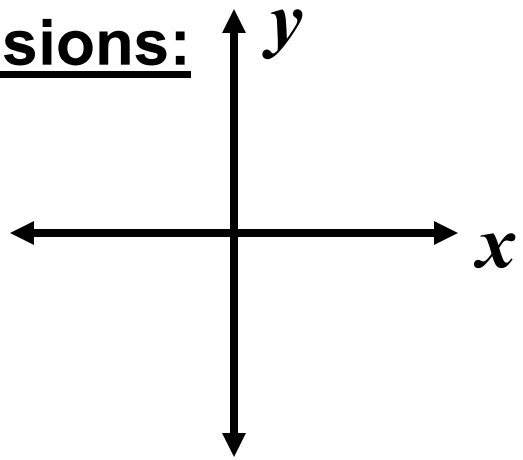
$$V = R\int_0^{2\pi} d\phi = 2\pi R$$

$$x^2 + y^2 = R^2$$

Spaces that obey the cosmological principle:

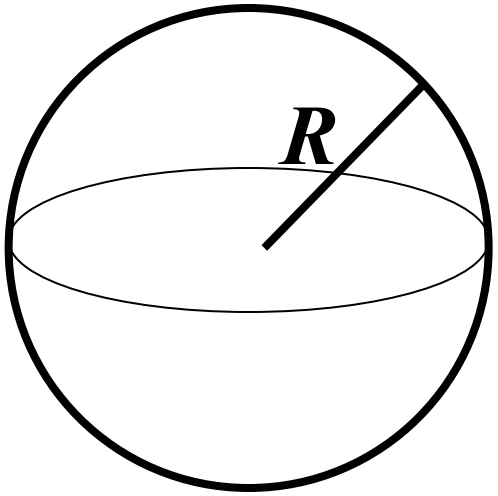
2-dimensions:

^2R



$$V = \int_{-\infty}^{\infty} dx \int_{-\infty}^{\infty} dy = \infty$$

^2S



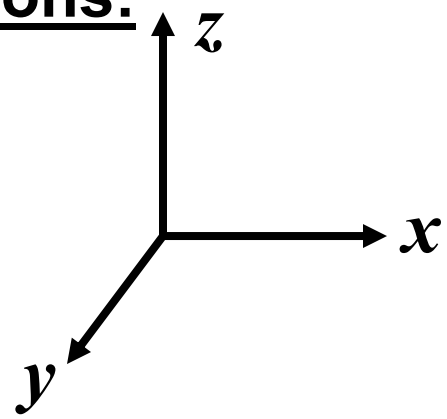
$$V = R^2 \int_0^{\pi} \sin\theta \, d\theta \int_0^{2\pi} d\phi = 4\pi R^2$$

$$x^2 + y^2 + z^2 = R^2$$

Spaces that obey the cosmological principle:

3-dimensions:

^3R

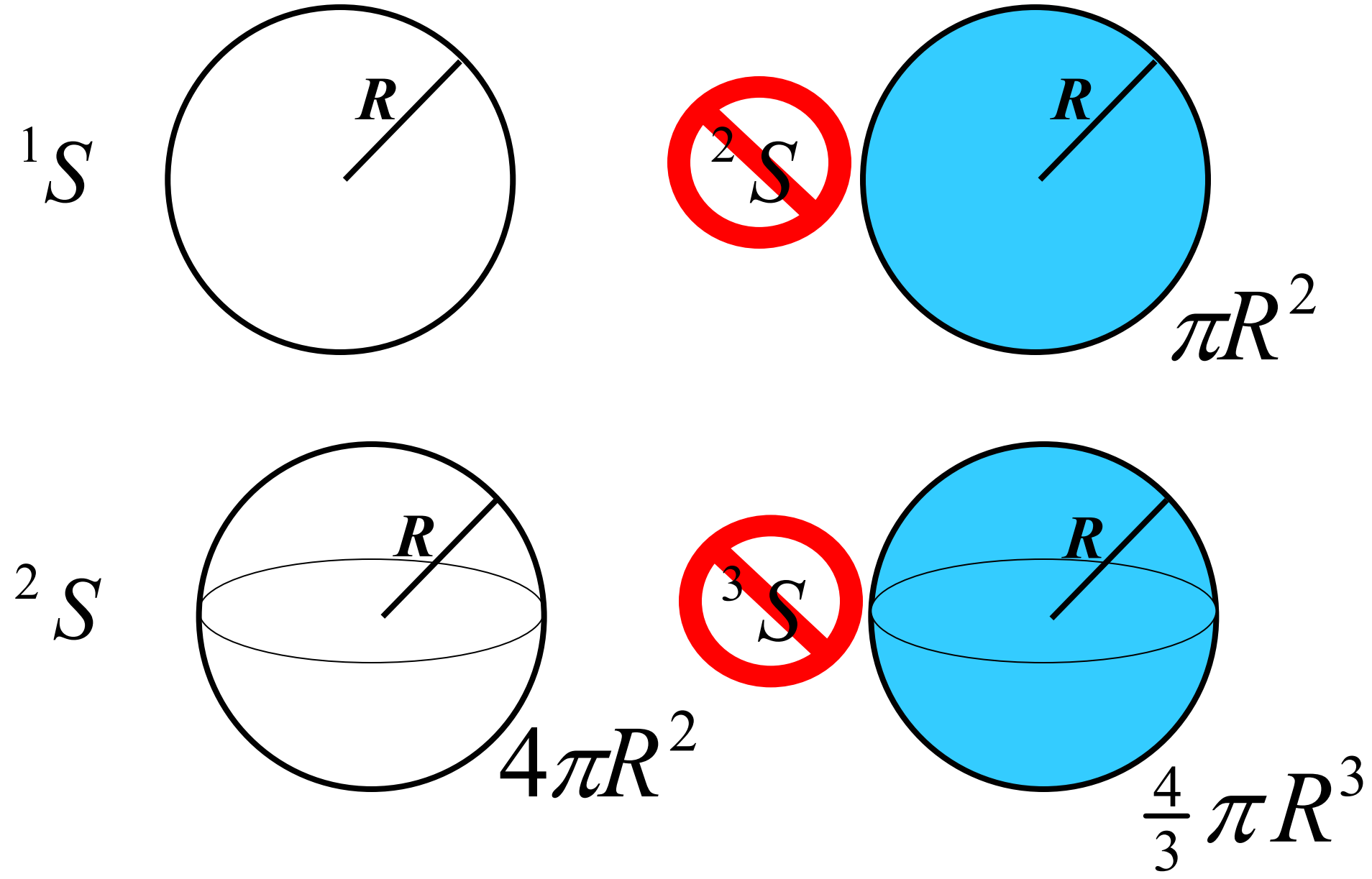


$$V = \int_{-\infty}^{\infty} dx \int_{-\infty}^{\infty} dy \int_{-\infty}^{\infty} dz = \infty$$

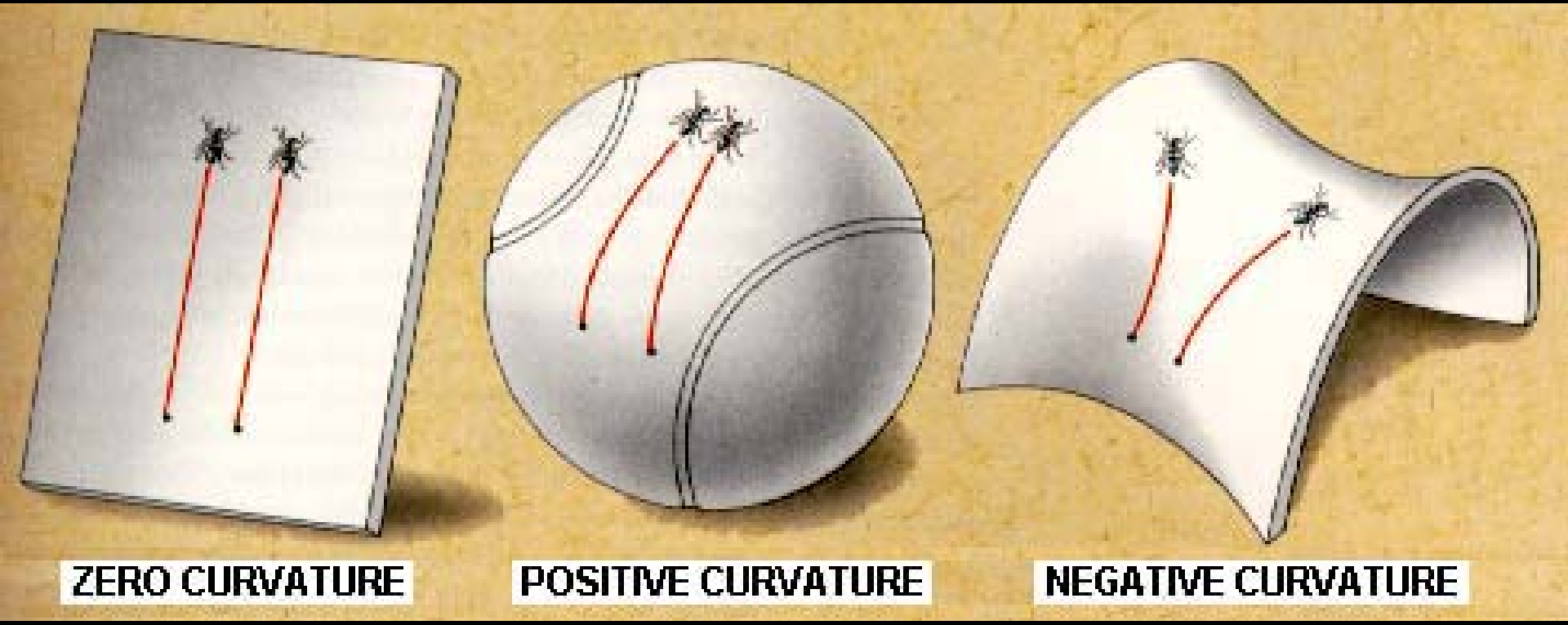
^3S

$$V = R^3 \int_0^{\pi} \sin^2 \chi \, d\chi \int_0^{\pi} \sin\theta \, d\theta \int_0^{2\pi} d\phi = 2\pi^2 R^3$$

$$x^2 + y^2 + z^2 + w^2 = R^2$$

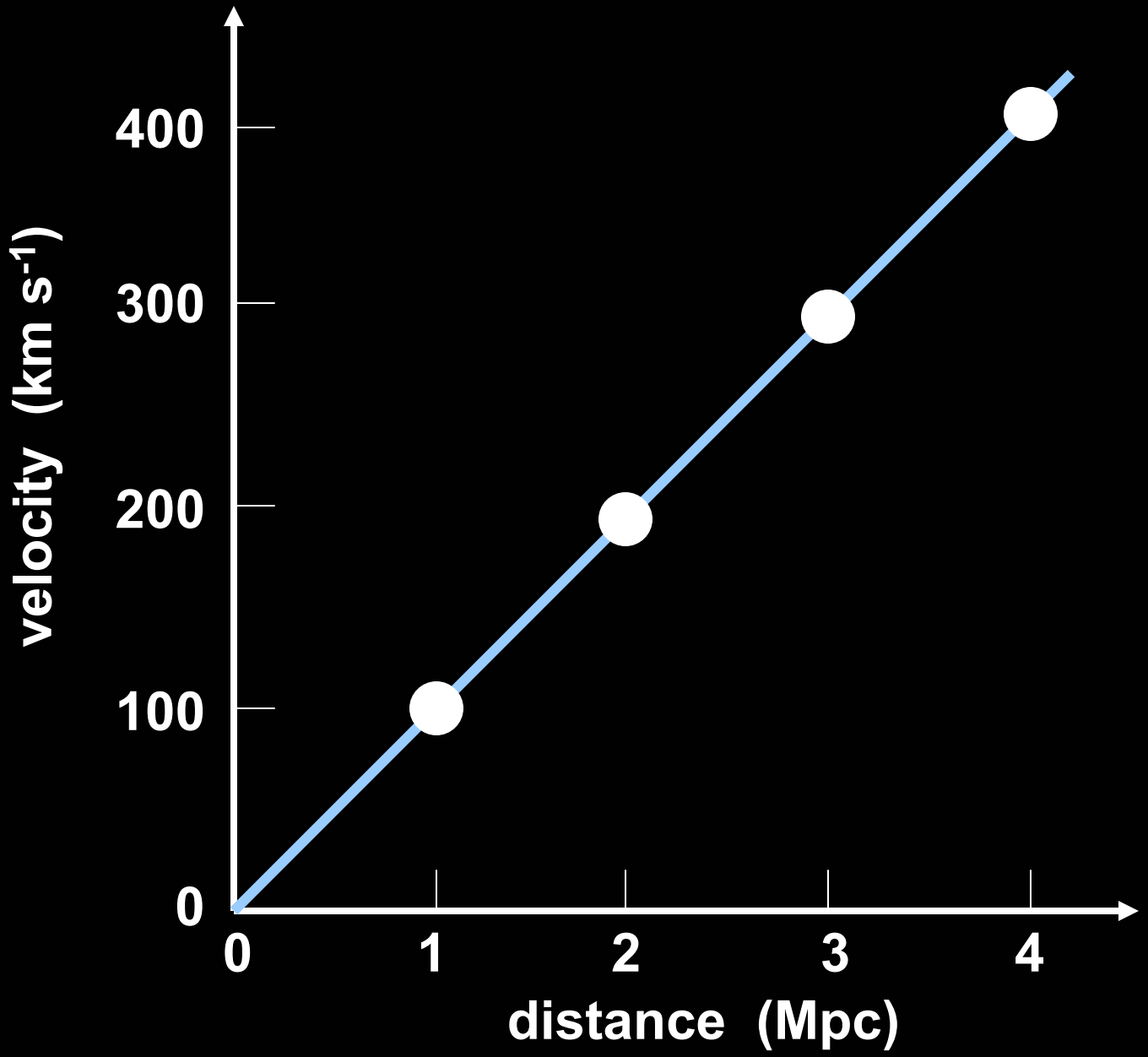

^1S
R
^2S
R
πR^2
^2S
R
$4\pi R^2$
^3S
R
$\frac{4}{3}\pi R^3$

^3R ^3S ^3H



FLAT SPHERICAL HYPERBOLIC

Hubble's Law: $v = H_0 d$ (H_0=100 km s^{-1} Mpc^{-1})



The expansion of the universe is

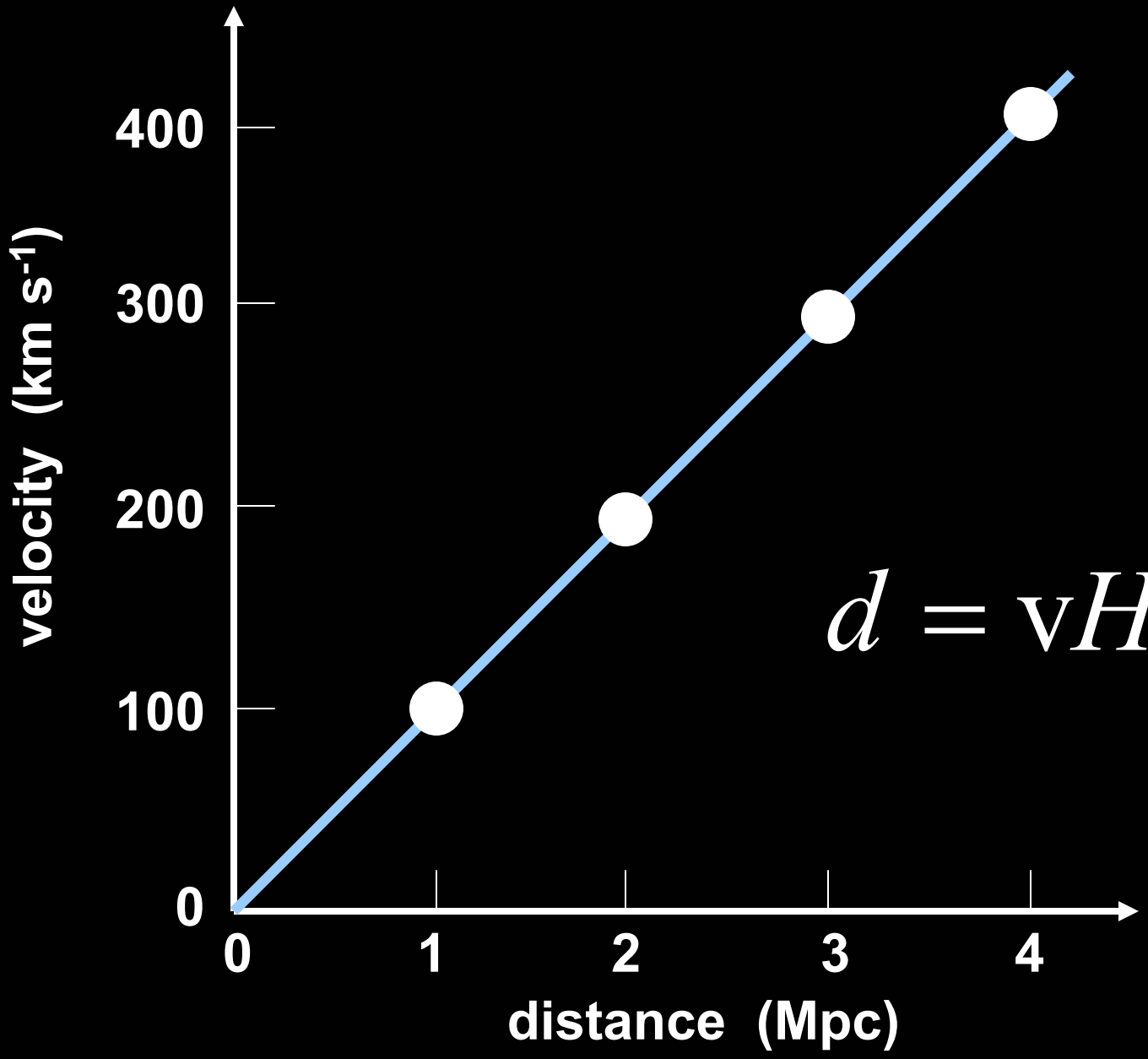
an explosion *of* space

not

an explosion *into* space

The universe does not expand *into* anything!

Hubble's Law: $v = H_0 d$ $(H_0 = 100h$ km s^{-1} Mpc$^{-1})$



The Hubble age of the universe

$$d = \mathrm{v}t \qquad \text{distance} = \text{velocity} \times \text{time}$$

$$d = \mathrm{v}H_0^{-1} \quad \text{Hubble's law}$$

$$\Big\} \; t = H_0^{-1}$$

$$H_0 = 100h \ \mathrm{km}\,\mathrm{s}^{-1}\,\mathrm{Mpc}^{-1} \times \frac{1\ \mathrm{Mpc}}{3\times10^{19}\ \mathrm{km}}$$

$$(0.8 \geq h \geq 0.6)$$

$$= \frac{100h}{3\times10^{19}}\,\mathrm{s} \times \frac{3\times10^{7}\ \mathrm{s}}{1\ \mathrm{year}}$$

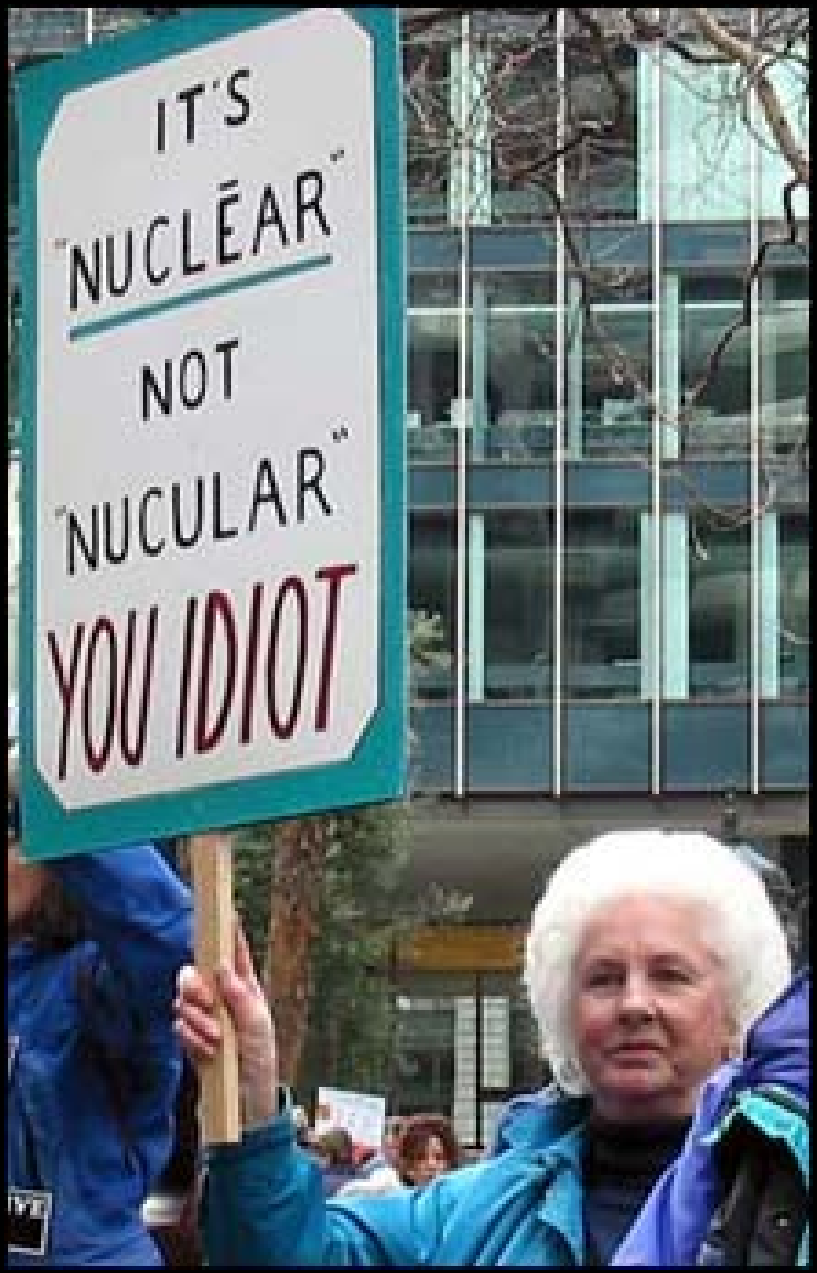
$$= \frac{100h}{10^{12}\ \mathrm{years}} = \frac{h}{10^{10}\ \mathrm{years}}$$

$$t = 10^{10}\,h^{-1}\ \mathrm{years}$$

$$12.5 \leq t \leq 17\ \mathrm{Gyr}$$

$$1\ \mathrm{Gyr} = 10^{9}\ \mathrm{years}$$

Nuclear Physics

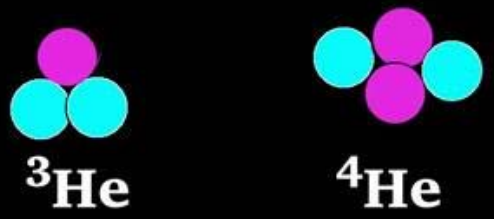


Nucleus made of

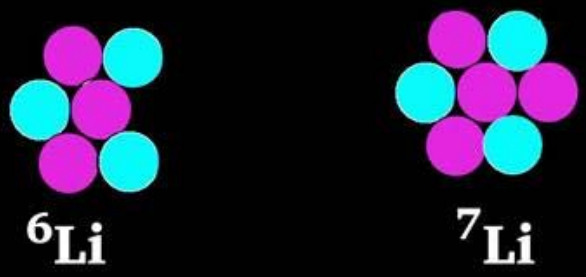
- protons – charge = +1
- neutrons – charge = 0

Hydrogen
1 proton

Helium
2 protons



Lithium
3 protons



The age of the elements

- Elements come in different isotopes
  (same # of protons, different number of neutrons)
- Many isotopes are radioactive — they decay
- If start with $N(0)$ nuclei, after a time *t*, the number will be

$$N(t) = N(0)\, 2^{-t/\tau_{1/2}}$$

$\tau_{1/2}$ is the half-life

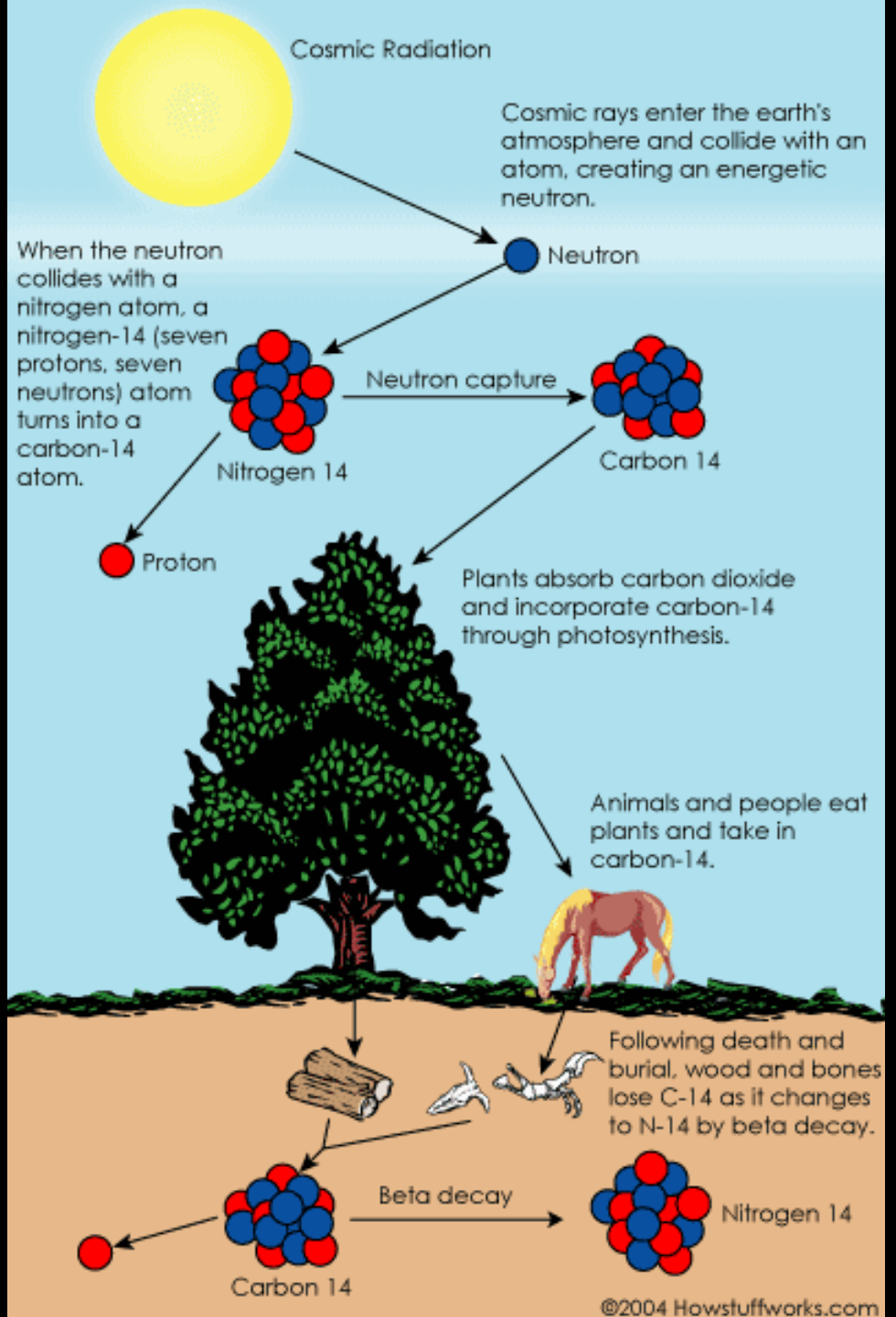
Can use radioactive isotopes to date objects
Radio dating …. nucleocosmochronology

Radiodating ^{14}C

Carbon has 6 protons
Nitrogen has 7 protons

$$n + {}^{14}\mathrm{N} \rightarrow p + {}^{14}\mathrm{C}$$

$${}^{14}\mathrm{C} \rightarrow \mathrm{e}^{-} + {}^{14}\mathrm{N}$$



^{14}C dating

- Carbon has two main isotopes ^{12}C and ^{14}C
- ^{14}C (6 protons + 8 neutrons) is unstable
  - half life of 5,746 years
- ^{12}C (6 protons +6 neutrons) is stable
  - it doesn't decay

$$N_{14}(t) = N_{14}(0)\, 2^{-t/5746\,\text{years}}$$

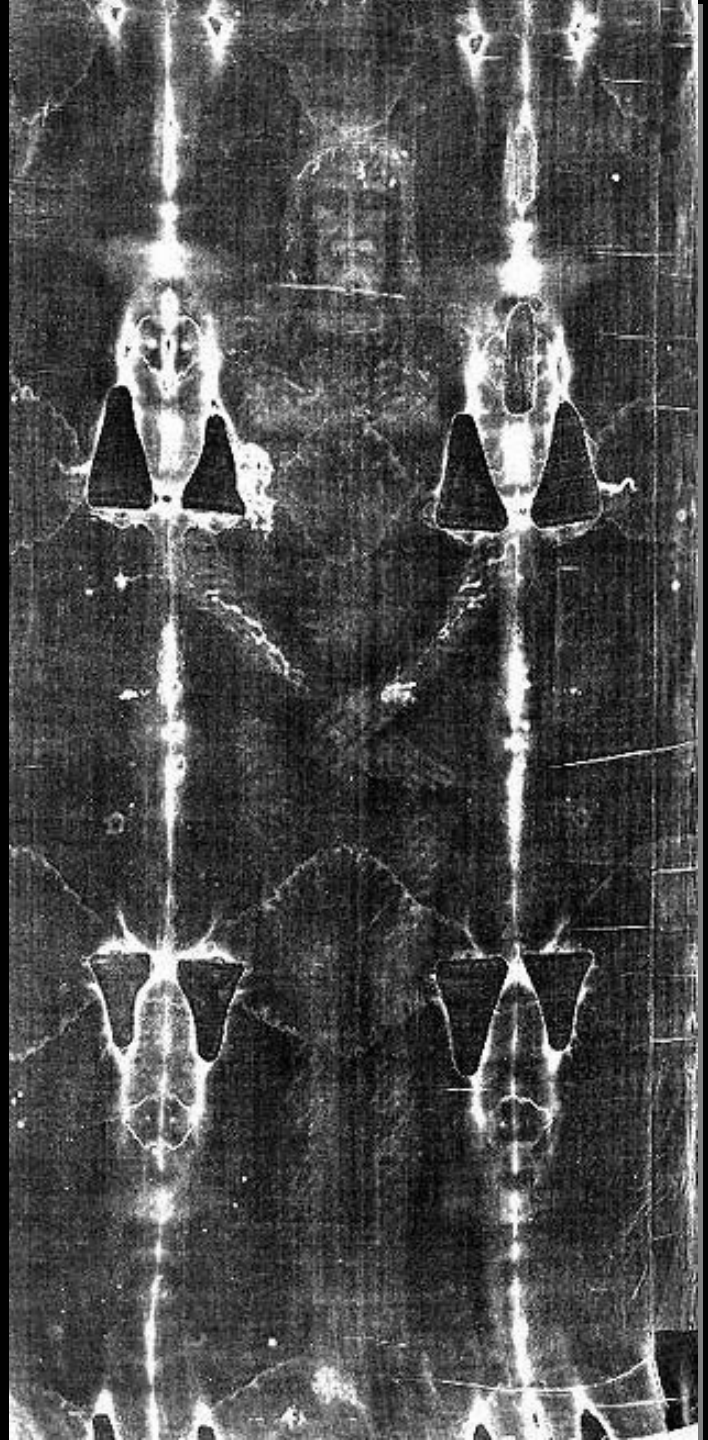
$$N_{12}(t) = N_{12}(0)$$

$$\frac{N_{14}}{N_{12}}(t) = \frac{N_{14}}{N_{12}}(0)\, 2^{-t/5746\ \text{years}}$$

Torino

il Duomo di Torino (1498)
la Cappella della Santa Sindone
e sullo sfondo la Mole Antonellian

Turin Cathedral,
Holy Shroud Chapel
and Mole Antonelliana



The Shroud of Turin


BILL ACOSTA
Flamingo
PALACE
TO Fabulous
LAS VEGAS
NEVADA

Caesar's Palace

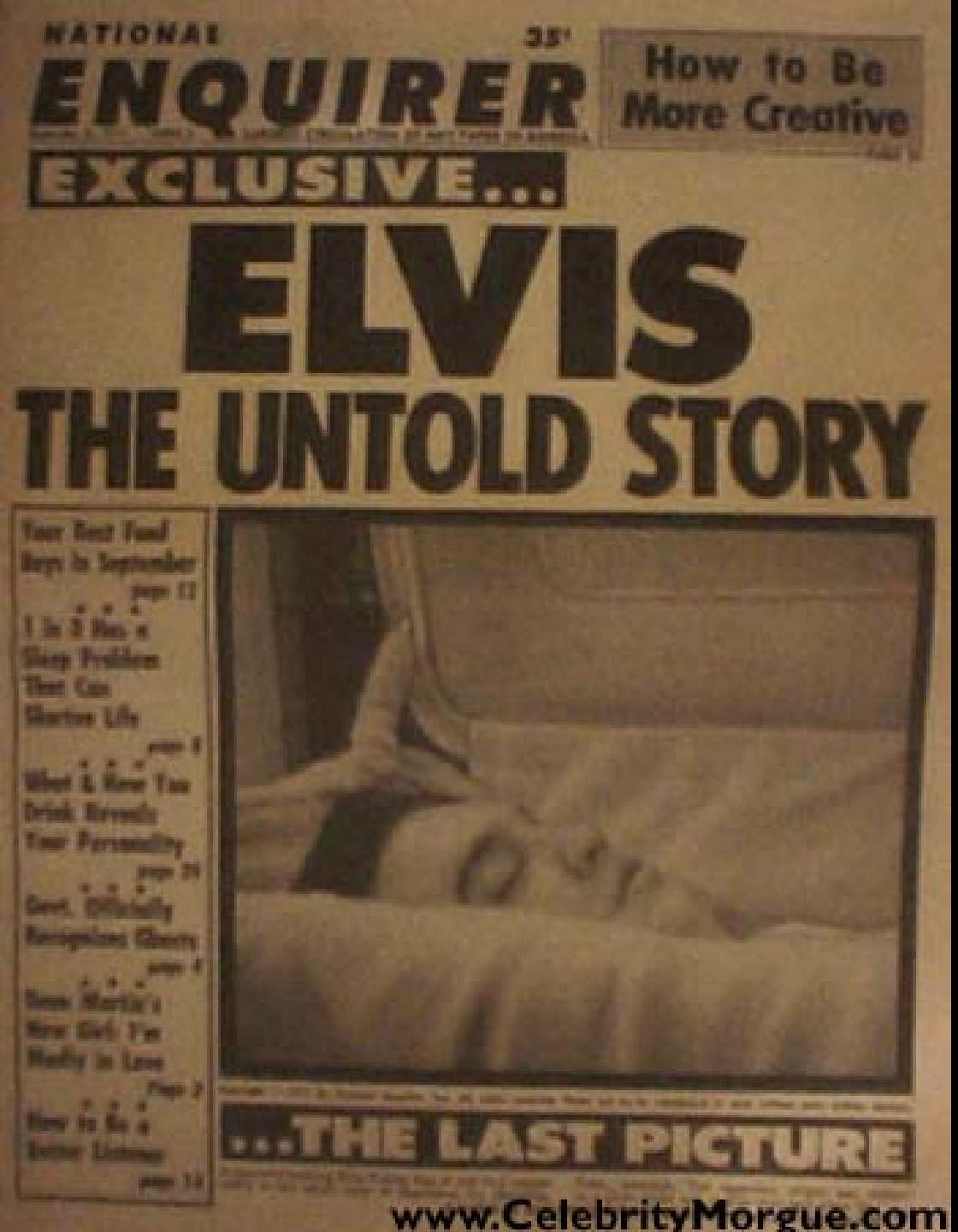
Shroud of Vegas

CSI: Hyde Park

Cosmological Scene Investigation

Task: Determine authenticity of Shroud of Vegas

- Re-enact scene of Elvis's (purported) death
- Examine evidence
- Use scientific tools (radiodating…not faith-based)



Death of Elvis

introducing

Felipe Marin as the King

The Shroud of Vegas—28 years old?

- Peanut butter contains ^{12}C and ^{14}C
- ^{12}C is stable and ^{14}C is unstable - half-life of 5,746 years

$$\frac{N_{14}}{N_{12}}(t) = \frac{N_{14}}{N_{12}}(0)\,2^{-28\text{ years}/5746\text{ years}}$$

$$= \frac{N_{14}}{N_{12}}(0)\,2^{-0.004} = 0.997$$

The Shroud of Vegas—28 years old?

- B-B-Q sauce contains ^{23}Na and ^{20}Na
- ^{23}Na is stable and ^{20}Na is unstable - half-life of 0.4 seconds

$$\frac{N_{20}}{N_{23}}(t) = \frac{N_{20}}{N_{23}}(0)\,2^{-28 \text{ years}/0.4 \text{ seconds}}$$

$$= \frac{N_{20}}{N_{23}}(0)\,2^{-1{,}811{,}250{,}000} \approx 0$$

The Shroud of Vegas—28 years old?

- Brylcreem contains ^{1}H and ^{3}H
- ^{1}H is stable and ^{3}H is unstable - half-life of 12.5 years

$$\frac{N_3}{N_1}(t) = \frac{N_3}{N_1}(0)\,2^{-28\text{ years}/12\text{ years}}$$

$$= \frac{N_3}{N_1}(0)\,2^{-2} = \frac{N_3}{N_1}(0) \times \frac{1}{4}$$